

Design And Analysis Of Formula Sae Vehicle Rear Upright Andcomparison Of Analytical And Software Analysis Solutions Ofprincipalstressesat Differentpoints

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Abstract:Upright is used in vehicles which connects frame or chassis and tires. Chassis is connected toupright with A-arms at the top and bottom using different types of fasteners through which theload is transmitted to it. I choose to design a FSAE(formula society of automobile engineers) caruprightbasedonthedatacollectedfromarealtimehybridformulavehicle.Uprightismodeledin Solidworks 2015 and all principle stresses and strains are found through simulation analysissoftware ANSYS 19.2. Now these solutions are compared with the analytical solutions which issolved using MATLAB software, So that we can be able to predict which one is more accurateandhowthese simulationsoftwareare beingableto solveproblemsbased ontheseconcepts.

1. Introduction

A major component of the vehicle suspension system which allows the steering arm to turn the front wheels and support the vertical load of the vehicle. It is also known as knuckle. upright is one which connects steering arms, control arms, springs, brake calipers, tires and in case rear upright then it also connects axles as shown in fig.1. It provides adjustment of different suspension parameters like steering Ackerman geometry, caster, camber and scrub radius [1]. The forces encountered by the car due to road and tire interactions go through upright, so the upright should be stiff and strong to withstand high forces. Also be able to withstand failure at the time of crashing or other emergencies because the failure of upright makes the car un-drivable. Car upright is subjected to fatigue load, braking force, cornering force, impact load during its service life [2]. The upright or knuckle design determines the geometry on the suspension's "outboard" side. (The mounting points on the chassis and wishbones / links form the "inboard" side of the suspension and make their own contribution to the overall geometry of the suspension.)

The fig.1 illustrates an example of a non - driven independent wishbone suspension. The upright (Yellow) is attached to the car using the upper and lower wishbones which have fasteners (ball joints or rod ends). This allows the upright to rotate about the king pin axis and move vertically.

Part attached to the upright is the spindle (green). Bearings (Orange) are inserted into the hub (Red) and it slides over the spindle and held in place by a retaining nut. The brake disc (Blue) is placed over the threaded bolts extending from the hub. The brake caliper (Light blue) is attached using a bracket to upright.

The steering angle of the upright can be set using the steering/toe link which has a rod end that fastens using ball joint to an arm (Purple) on the upright.

DESIGN AND ANALYSIS OF FORMULA SAE VEHICLE REAR UPRIGHT AND COMPARISON OF ANALYTICAL AND SOFTWARE ANALYSIS SOLUTIONS OF PRINCIPAL STRESSES AT DIFFERENT POINTS

Non-Driven Wheel Upright

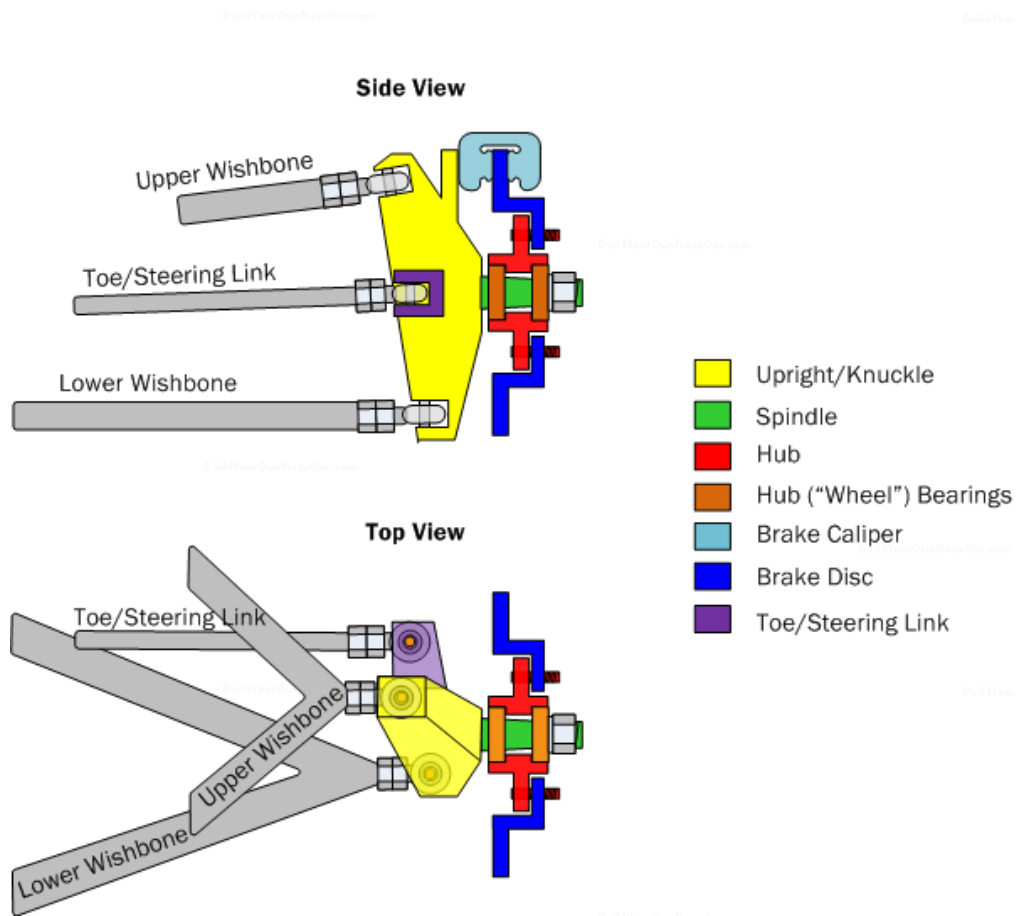


Fig.1 side and top view of an upright attached to a wishbone suspension [3]

➤ Before designing an upright we need to know the following suspension parameters which are based on the alignment of a vehicle such as:

2. Camber angle

It is the angle measured between the wheel vertical alignment normal to its surface. If the wheel is perpendicular to its surface then its camber angle is 0 degrees. It is described as negative when top of the wheel begins to tilt inward that means towards the vehicle whereas the tire tilts

outwards it is positive camber angle [4]. Most vehicle have neutral camber angles and most racecars have negative camber angle. Negative camber have more grip advantage during corneringthushavinggood handling whereasin neutral camber itresults in tire wear.

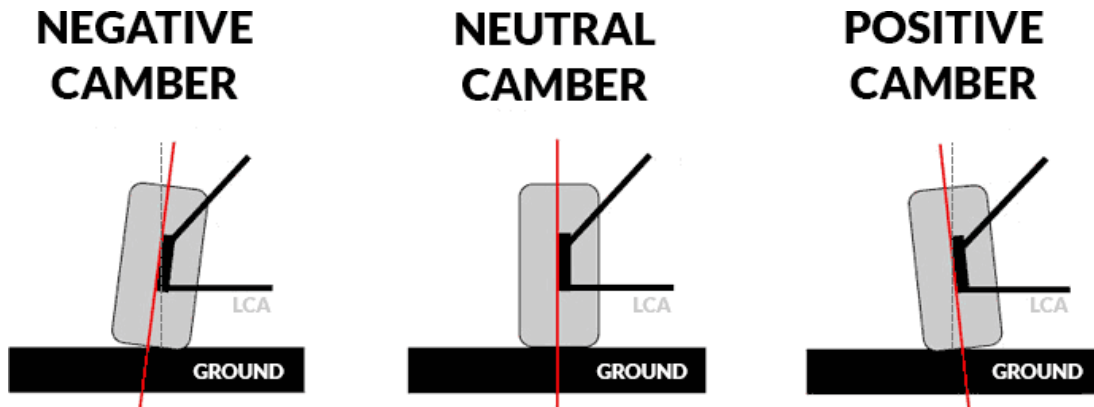


Figure.2Differentcamberangles[5]

3. Casterangle

4. It is the measure of angle between the steering axis and vertical axis from the side view as shown in fig.3. when both the axis are in same angle then it is neutral caster. when the top of steering angle moves forward it is negative angle and vice versa. most vehicles have positivecasterasitmakesstable at highspeeds and increases steeringstability [4].

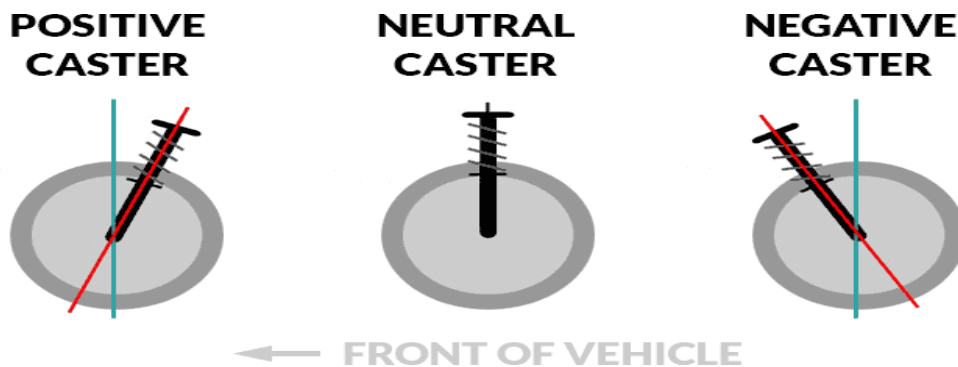


Figure.3Differentcasterangles[5]

5. Otherparameters

The kingpin inclination is the line formed when joining the lower ball joint(LBJ) and upper balljoint(UPJ). It is used to determine the camber and caster angle based on the kingpin inclination[5]. The distance kingpin inclination is offset from the tire center line is called scrub radius as shown in Fig.4.

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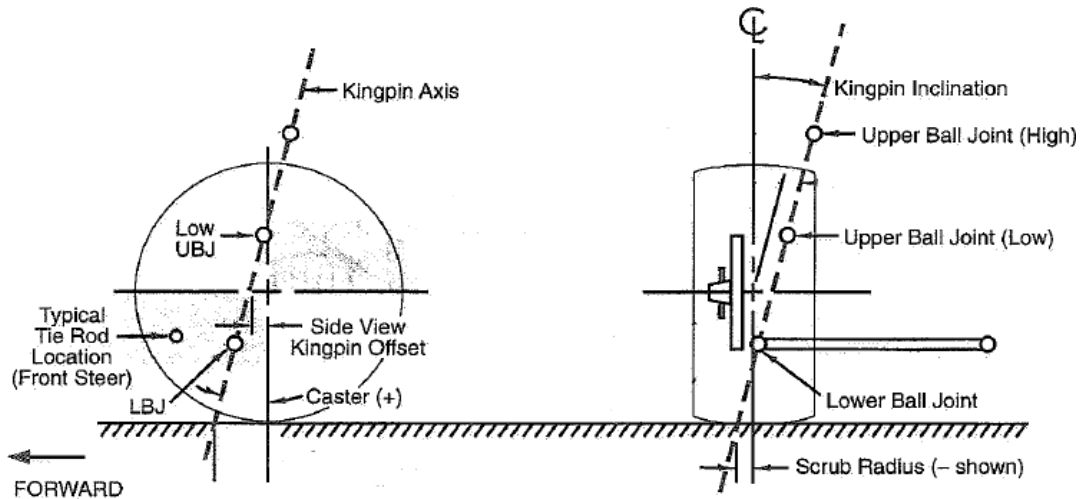


Figure.4 Kingpin inclination and scrub radius [6]

6. LITERATURE REVIEW

The service life of an upright is based on its dynamic conditions like fatigue loads always apply on the upright during jounce and bounce. Longitudinal loads are applied when it is in static and lateral loads are being applied when during braking and centrifugal forces act during cornering of vehicle [1].

While doing analysis we need to take consideration of camber and caster angle which is considered as 6° and then the loads are applied on it. Also the forces acted by wheel bearing is not taken in to consideration while doing the analysis. The upright for doing static analysis is considered there as it is easy to consider by eliminating the forces acted by the shaft [8].

Weight is one of the important consideration for a race car component mainly upright as it comes under unsprung mass. So optimization of design is important and also the selection of material which gives us the actual weight of the component whereas it should be rigid to withstand $1/4^{th}$ of car's sprung mass and three times gravity acting on it during longitudinal loading [9].

7. DESIGN OF UPRIGHT

Design considerations

We consider various parameters while designing a component. Irrespective of other details the major design parameters determine the performance of upright.

The parameters that are considered while designing the upright is:

1. Castor angle along the vertical axis of the upright is 6° .
2. It should have a brake caliper mount on one side of the upright and the steering rack mount should be on the opposite side.
3. Bores should be provided on the top and bottom of upright to accommodate the ball joints.
4. Sufficient wall thickness to make the component strong and stiff to withstand the weight of vehicle.
5. Length of upright should be considered as it should fit in the wheel hub.
6. Weight is an important parameter as it helps for fuel economy and good handling performance as well as more acceleration.

In order to design a upright you have to consider all the suspension parameters such as wheel dimensions, the estimated weight of whole vehicle, track width, wheel base. This following data is taken from a Formula hybrid vehicle team.

Wheelbase	68 in
Overall length of vehicle	116 in

Trackwidth	Front:48in
Tires	R13 155 65
Massofvehicle	470 kg
Groundclearance	2 in
suspension	Doublewishbonedampertolowerwishbone

Table.1 Suspension parameters

8. Materialselection

After studying the comparison made in the table below an easy discussion can be made that AISI1018 is the suitable material as it is having better weight to strength ratio at a reasonable cost in comparison to other materials.

Material	Ultimate strength(MPa)	Yield strength(MPa)	Density(g/cc)	Strength	Cost/meter \$
AISI1018	350	340	7.87	55-60	4.12
AISI1020	380	370	7.87	60-62	6.2
AISI4130	410	400	7.85	70-75	8

Table.2 Material properties comparison

9. Forces acting on an upright

- Longitudinal force during braking.

While braking the weight on rear side tends to come to front side of the vehicle. So there is load transfer takes place from rear to front.

Force at the front side = mass at the rear side * acceleration

Let the rear side of the vehicle be 0.6 times the total weight = 0.6 * 470 = 282 kg

Force is considered for worst case conditions and 4g loads are applied on the upright. Force = 282 * 4 * 9.8 = 110544.4 N

Force on 1 wheel = 110544.4 / 2 = 55272.2 N

- Lateral forces

Lateral forces are because of two reasons centrifugal forces and lateral load transfer from outside to inside while turning.

Turning radius = 3m V = 30 kmph = 8.33 m/s

Centrifugal force = $mv^2/r = (0.4 * 470 * 8.33^2) / 3 = 4348.37$ Lateral load transfer = 0.4 * 470 = 188 kg

Force = 188 * 3 * 9.8 = 5527.2 N

lateral Force for one wheel = 2763.6 N

Force acting on caliper mounts = torque / radius = 58000 / 110 = 527.27 N

10. MODELING

upright is modeled in Solid works 2015 software, which is used for designing, drafting and as well as analysis of different components. It is developed by Dassault Systems. Using all the design considerations and based on the hybrid formula rule this upright is being modeled.

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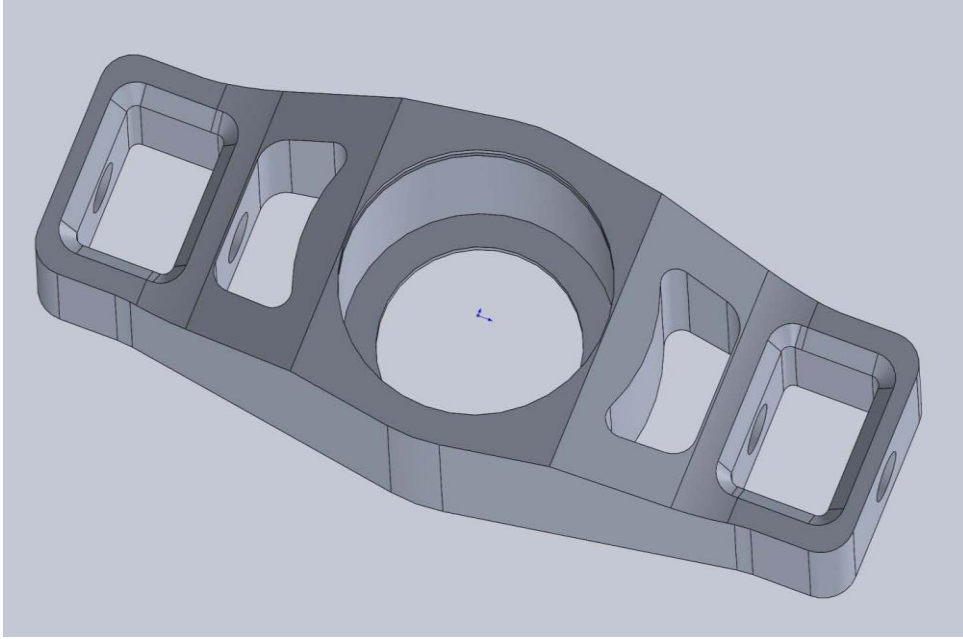


Figure.5 Upright designed using Solidworks

As shown in figure.6 we can see the cross section area where the lateral and longitudinal forces are applied. They are applied along the axis so while applying the forces the axis is being rotated in Ansys and then the forces are applied.

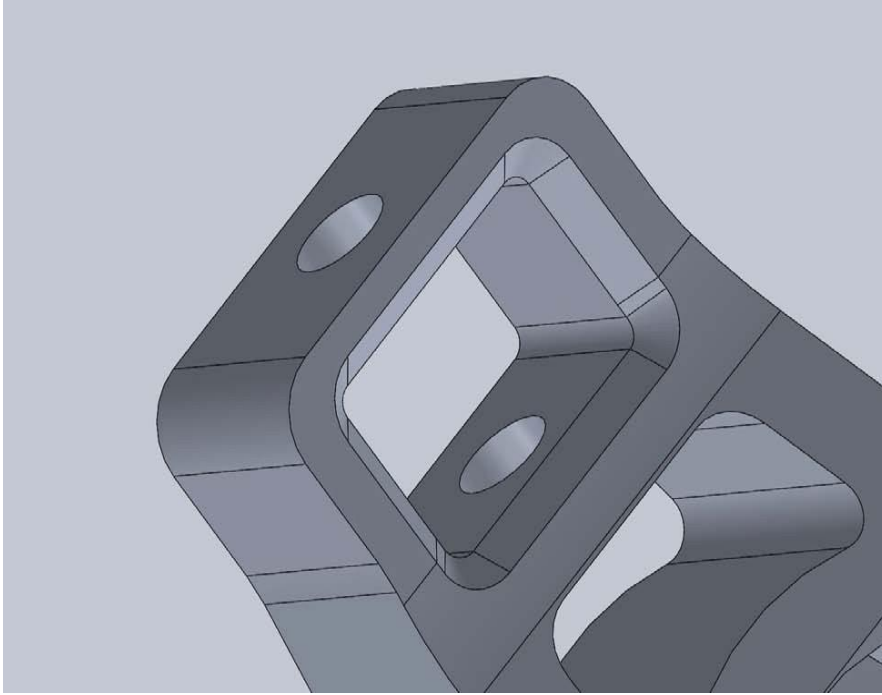


Figure.6 Cross-sectional area

11. THEORITICAL CALCULATIONS

Stress is a measure of external force acting on the cross sectional area of a component or body. Stress has a unit of N/m^2 . There are two types of stress 1. Normal stress - when force acts perpendicular to surface and other one is 2. Shear force - when force acts parallel to surface of an object.

$$\sigma = \frac{p}{A}$$

When we consider this equation there are lots of assumptions. They are - we assume all materials are homogeneous, isotropic and elastic as well as object as prismatic meaning the cross-section will be same along its length. Because of all these assumptions the object deforms uniformly at every point along its cross-section. Normal stress at a point on a cross section is defined by (with similar equations in the y and z directions) [10].

$$\frac{\Delta F_x}{\Delta A_x}$$

$$\sigma = \lim$$

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$$\lim_{\Delta A \rightarrow 0} \Delta A$$

Every small area is subjected to similar forces, and the sum of all the forces should be equal to resultant forces. We integrate both sides of the equation and arrive at a relationship for normal stress.

$$dF = \sigma dA$$

$$\sigma dA$$

$$\therefore p = \sigma A$$

So we use the above equation to find out σ_x and σ_y using the area on which the stress acts upon.

$$\sigma_x = 3.83 \text{ MPa} \quad \sigma_y = 2.87 \text{ MPa}$$

12. Finding principle stresses

As the caster angle is applied so now the upright is rotated with 6° and then we find the principle stresses and also the shear stress formed on upright using equation (1) and (2). These equations are being solved using MATLAB.

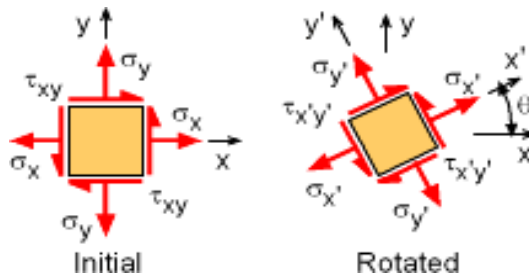


Figure.7 Rotating stresses to x-y coordinate to x'-y' coordinate system [11]

$$\sigma_{1,2} = \frac{\sigma_x + \sigma_y}{2} \pm \sqrt{\left(\frac{\sigma_x - \sigma_y}{2}\right)^2 + \tau_{xy}^2} \quad (1)$$

$$\tan 2\theta_p = \frac{2\tau_{xy}}{\sigma_x - \sigma_y} \quad (2)$$

13. STATIC STRUCTURAL ANALYSIS

ANSYS

It is a simulation software package where it solve different governing equations to do the static structural analysis as well as other simulations. They solve these equations by dividing the component to number of small parts this process is called meshing where as it is a finite element analysis. The results can be obtained in various formats. As we are not able to do structural analysis for complex structures with different kinds of loads applied on model so we use ansys to do simulations over the complex structures.

Steps to do a structural analysis in ansys:

1. Select a chosen material from the engineering data.
2. Create geometry or import its geometry file from solidworks.
3. We should do fine mesh to get accurate results after simulation.
4. After meshing, different types of loads are being applied on the upright and the results are being obtained as seen below.

The upright is rotated 6° around the Z-axis as we need to find principle stresses when the caster angle is in 6° angle. This is being done in ANSYS software setup.

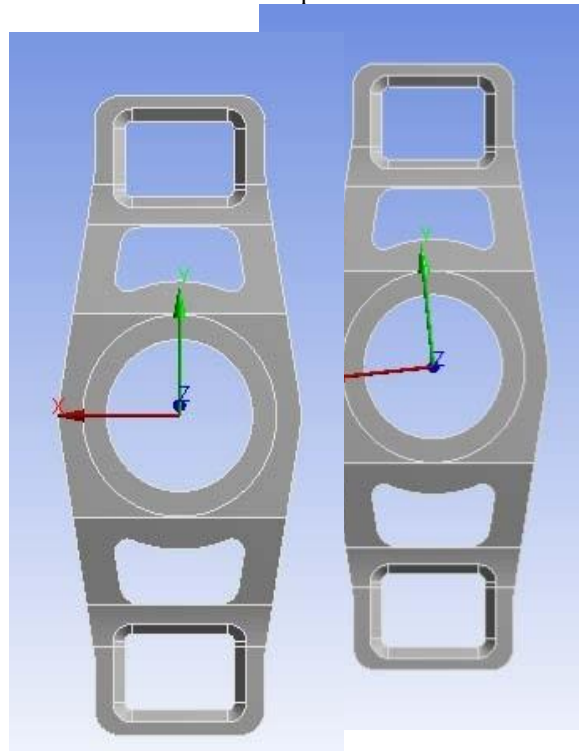


Figure.8 Rotation of axis in Ansys

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Meshing

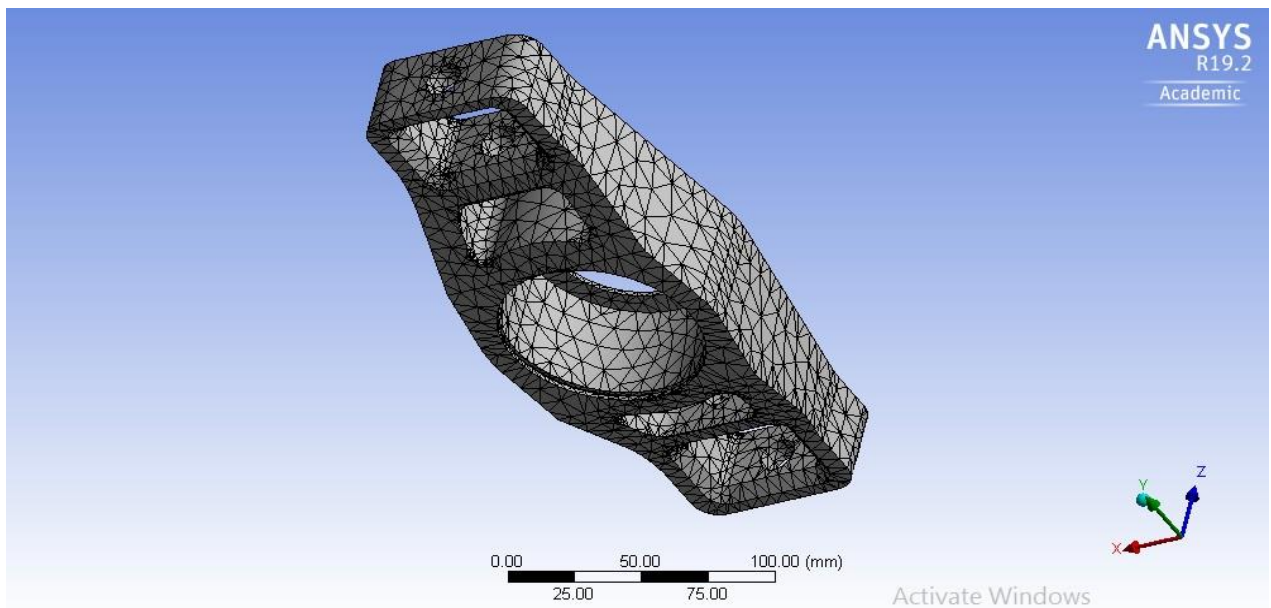


Figure.9 Meshing with element size 6mm

Element size	6.0mm
No. of nodes	23261
Refinement	Fine

Table.3 Mesh information

Forces applied in longitudinal and lateral directions

A: Static Structural
 Fixed Support
 Time: 1. s
 06-Apr-19 8:33 PM

- A** Force: 5527. N
- B** Force 2: 2763. N
- C** Fixed Support

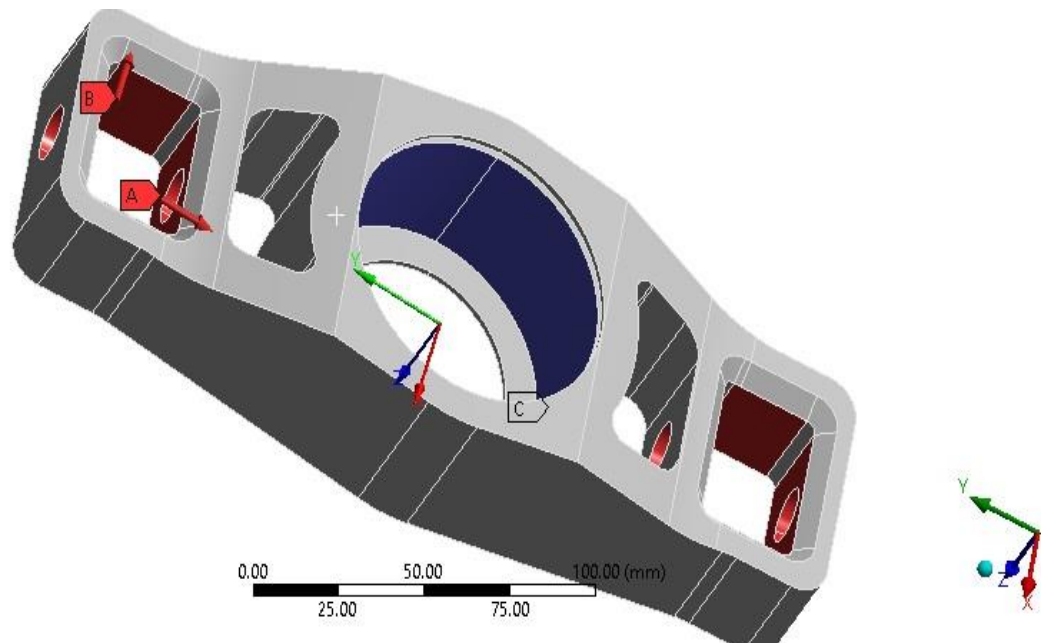


Figure.10 Forces applied during zero caster angle

A: Static Structural
 Fixed Support
 Time: 1. s
 06-Apr-19 7:36 PM

- **A** Force: 5527. N
- **B** Force 2: 2763. N
- **C** Fixed Support

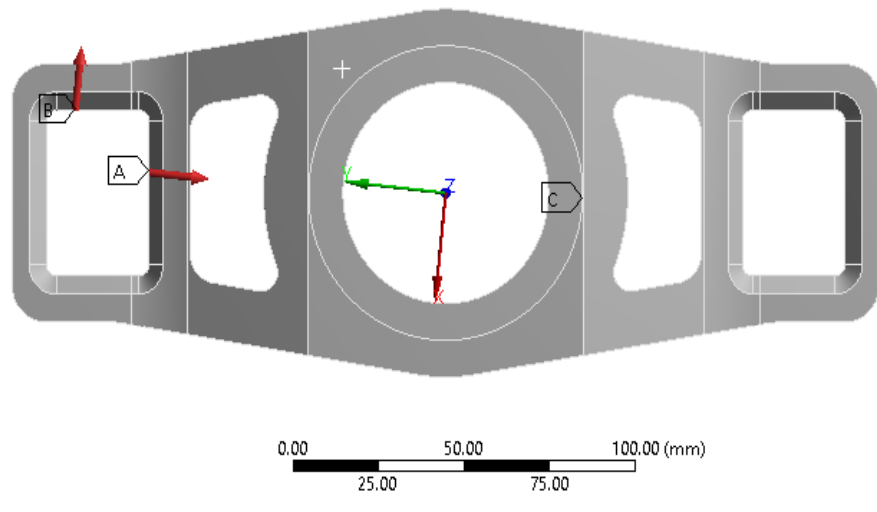


Figure.11 Forces applied during positive caster angle (After rotation)

Total deformation at zero caster

A: Static Structural
 Total Deformation
 Type: Total Deformation
 Unit: mm
 Time: 1
 06-Apr-19 7:39 PM

- **0.0094789 Max**
- 0.0084257
- 0.0073724
- 0.0063192
- 0.005266
- 0.0042128
- 0.0031596
- 0.0021064
- 0.0010532
- **0 Min**

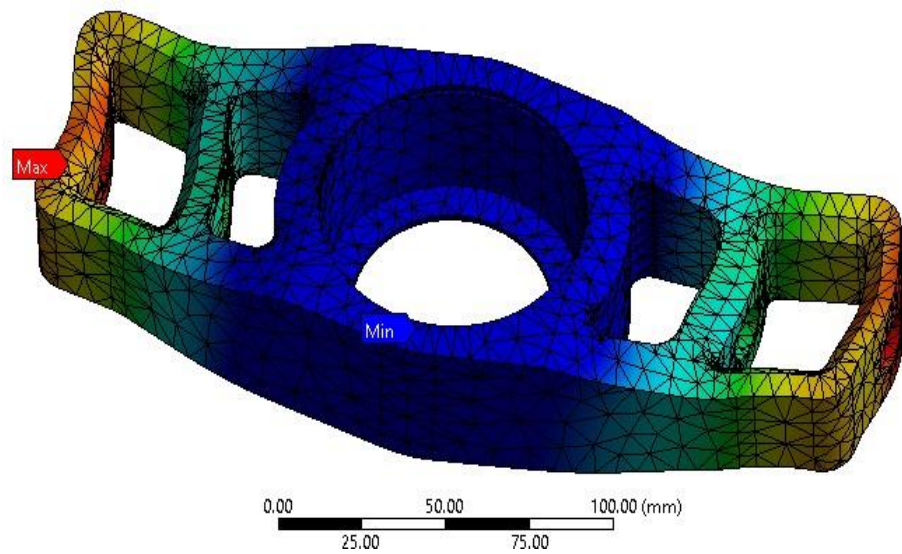


Figure.12 Total deformation on upright

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After the rotation of axis through the z-axis with 6° the loads are being applied as seen in figure. 11. We can see the decrease of deformation value when compared to right at zero degree angle in figure. 13.

Total deformation at positive caster (After rotation)

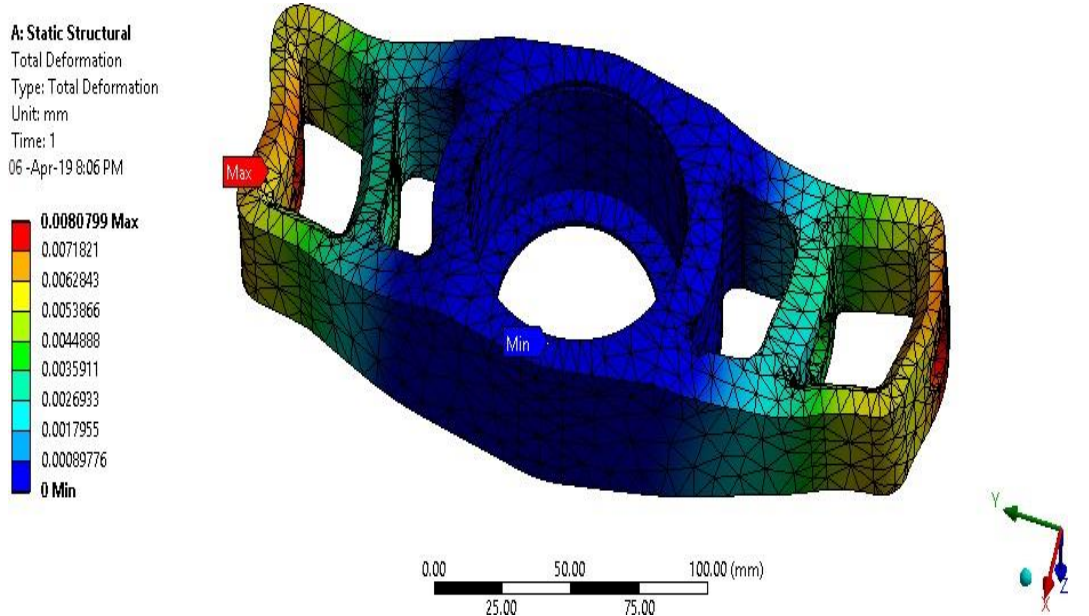


Figure.13 Total deformation on upright

Stress distribution at zero caster

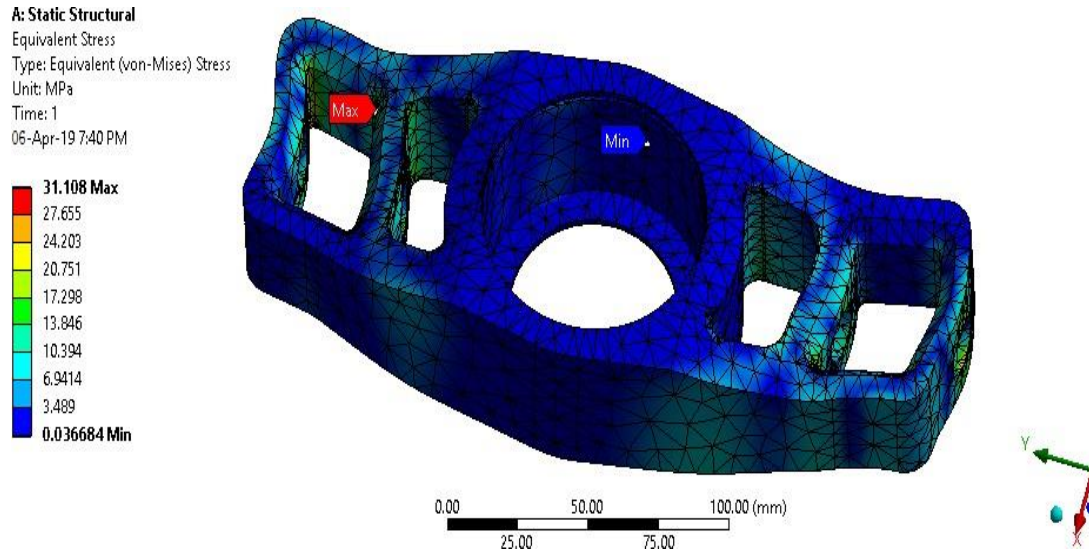


Figure.14 Von-Mises stresses

Stressdistributionatpositivecaster(Afterrotation)

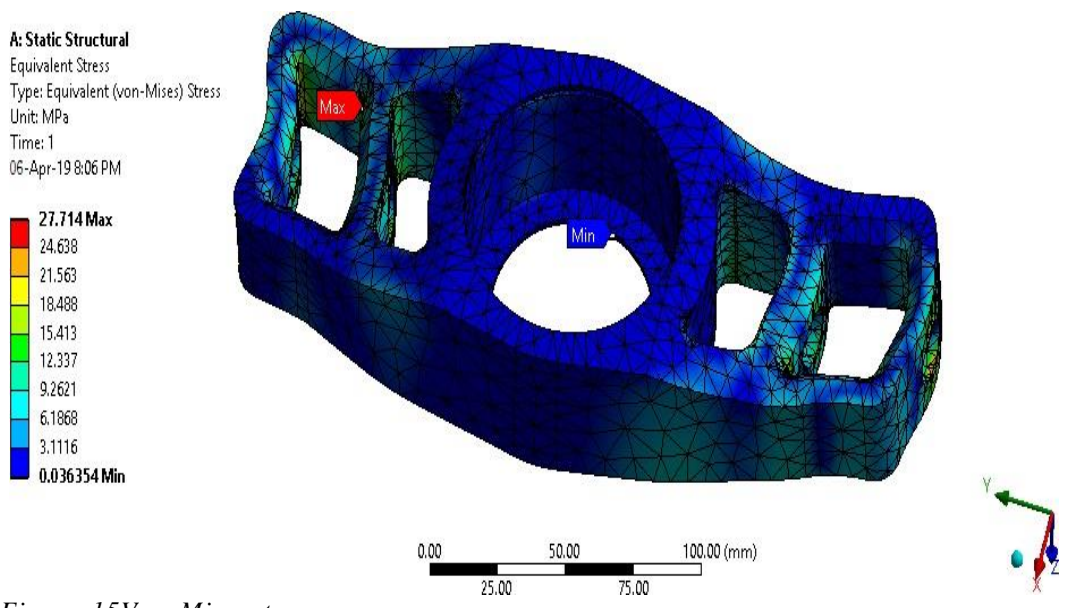


Figure.15 Von-Mises stresses

Findingfactorofsafety

Hereweareusingmaximumdistortionenergytheorytofindfactorofsafetyforchassis.According to this theory when the material is subjected to biaxial or triaxial stress it will fail onlyif maximum shape distortion energy is greater than shape distortion energy of specimen.(thistheoryis generally usedfor ductilematerials).

$$= \left[\frac{\sigma_1^2 + \sigma_2^2 - \sigma_1 \sigma_2}{\sigma_{yt}^2} \right]^{1/2} \times fos$$

σ_{yt} = yeildstrengthofmaterial
 σ_1 = maximumstress
 σ_2 = minimumstress
 fos = Factorofsafety

	σ_1 (Mpa)	σ_2 (Mpa)	Fos
Upright(Atneutralcaster)	31.1	0.036	8.36
Upright(At positive casterof6°)	27.71	0.036	9.02

Table.4Factorofsafety

14. RESULTS AND DISCUSSION

A: Static Structural

Equivalent Stress
 Type: Equivalent (von-Mises) Stress
 Unit: MPa
 Time: 1
 07-Apr-19 12:28 AM

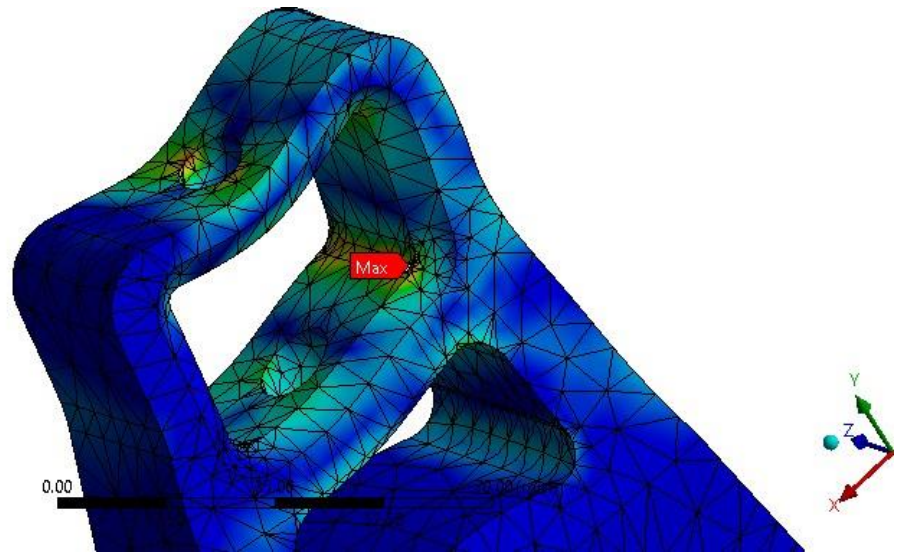
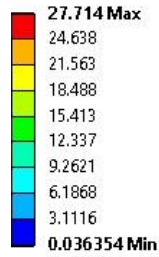


Figure.16 Max stress acting point

We can see the max stress acting at the corner where the area of longitudinal and lateral forces applied are meet, as shown in figure.16 and also we can see the maximum stress decrease when the transformation of angle takes place as the shear stress is developed in the component. Whereas rest of the area of component has a feasible stress which is near to the minimum stress obtained in the stress vector plot.

A: Static Structural

Equivalent Stress
 Type: Equivalent (von-Mises) Stress
 Unit: MPa
 Time: 1
 07-Apr-19 1:49 AM

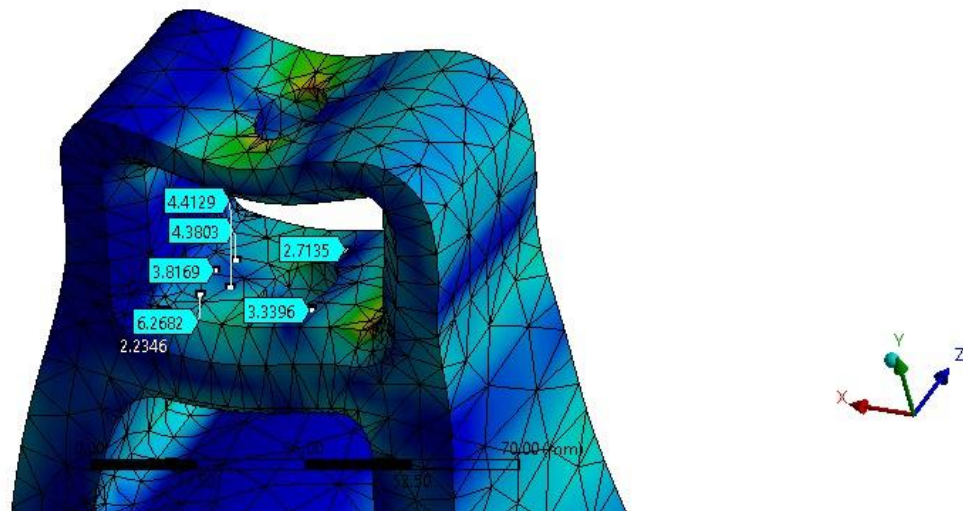
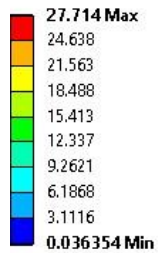


Figure.17 Stress at different points

Stresses at probes(MPa)	LocationX	LocationY	LocationZ
3.8169	11.370683	82.519946	9.599767
4.3803	9.629474	82.002066	13.350872
6.2682	10.525925	82.763561	3.099029
4.4129	7.047330	81.974359	6.932136
2.7135	-8.104269	82.389498	19.559983
3.3396	-8.104269	84.282837	2.133707

Table.4 Coordinates of probe points

As the objective of the project is to compare analytical solution with analysis software solutions we can obtain approximate results at the surface where the forces are applied because of this reason we have obtained $\sigma_x = 3.83$ and $\sigma_y = 2.87$. Whereas the rest of the body they have different stresses at different points as the lateral and longitudinal forces are applied at certain areas of the body and deforms non-uniformly.

Actually the comparison has few objections because the analytical calculations used to find the principle stresses are solved in 2D plane and are solved for infinitesimal element considering the same deformation takes place over the whole body. Ansys gives result based on the governing equations solved using finite element method.

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